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A RECOGNIZER FOR A PRECEDENCE GRAMMAR

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A RECOGNIZER FOR A PRECEDENCE GRAMMAR

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1. Introduction and definitions

This paper describes an algorithm which analyses a given string of symbols, stating whether the string belongs to the language generated by a given grammar or not. The recognizer represented here may be classified as a left-right, bottom-up recognizer, in the sense that the string is repeatedly searched from left to right until a substring is found which may be replaced by a certain symbol.

In order to describe the recognizer, some basic definitions are introduced here. The vocabulary V is a given set, the elements of which are called symbols. The vocabulary V is the union of A , the set of non-terminal symbols (represented here by the capital letters at the end of the alphabet: S, T, U , and so on), and B , the set of terminal symbols (represented here by the letters i, j, k , and, in case of special characters, by the characters themselves). A string of symbols is a finite sequence of symbols (either of the terminal or of the non-terminal type); strings will be represented by lowercase letters u, v, x, y, z . As a particular case, a string may be empty; this is the null string.

A production is defined as a relation of the form $S \rightarrow x$. The left part of a production is defined as the non-terminal (S) being defined; the right part of a production is the string (x) which defines the non-terminal. A phrase structure grammar is a finite set of productions with the following properties:

- a) x is a non empty string whose symbols belong to V ;
- b) S is a non-terminal symbol, belonging to A ;
- c) x can contain all the symbols in V , with one and only one exception, called the axiom.

A string z is a direct derivative of a string y if and only if there exists strings u, v (possibly empty) such that $y=uv$ and $z=uxv$, and also there exists a production of the form $U \rightarrow x$ in the grammar. A string z is a derivative of a string y if and only if there exists a sequence of strings x_0, x_1, \dots, x_n such that $y=x_0, x_0 \rightarrow x_1, \dots, x_{n-1} \rightarrow x_n, x_n=z$.

A parse of a string x with respect to the axiom S consists in a sequence of replacements made on the string x , each one substituting a substring by a certain non-terminal symbol. The parse is completed when a substring is replaced by the axiom S . A substring may be replaced when there exists a production $U \rightarrow y$ in the grammar, such that the string y is equal to the substring to be replaced. A canonical parse is defined as a parse in which at each time a replacement is to be made the substring to be replaced is the leftmost substring of the string being considered. The leftmost substring is called the handle. A grammar is said to be unambiguous if for each string x belonging to the language it generates there exists only one canonical parse.

The algorithm to be described here is based upon certain relations which may exist among the symbols belonging to V . These relations, called the precedence relations, are derived from the set of productions which ~~consists~~^{exist} in the grammar of the language. A grammar for which the relation between any two symbols is unique is called a precedence grammar.

Now that the necessary terminology is ^(a)available, the recognizer can be described in more details. The recognizer will try to execute, by means of successive steps, the canonical parse of the given string; then, at each step, the first action to be taken is the search for the handle. When it is found, it is replaced by the corresponding non-terminal symbol and the process continues. The handle can be easily found if we use the precedence relations mentioned earlier. The relations are stored in a matrix, and are of the following types:

a) between all adjacent symbols in the handle, relation \neq holds;

- b) between the leftmost symbol of the handle and the symbol immediately preceding the handle, relation \leftarrow holds;
- c) between the rightmost symbol of the handle and the symbol immediately after the handle, relation \rightarrow holds.

Once the precedence matrix is constructed, the process of finding the handle and reducing the string becomes very simple; it consists in a scan on the string searching a pair of successive symbols for which the relation \rightarrow holds; when such a pair is found a scan is made leftwards looking for a pair of adjacent symbols with the relation \leftarrow . All the symbols belonging to the substring so delimited are part of the handle and may be replaced. The process is then repeated until the last replacement is made yielding the axiom; in this case, the given string belongs to the language. The subsequent sections will provide a detailed description of the process, together with some restrictions made on the acceptable grammars and strings.

2. The precedence Matrix

The precedence relations can be defined in the following way (see Ref.1).

- a) For any ordered pair of symbols (S,T) relation $S \doteq T$ holds if and only if there exists a production of the form $U \rightarrow x S T y$, for some non-terminal U and some (possibly empty) strings x, y.
- b) For any ordered pair of symbols (S,T) relation $S \leftarrow T$ holds if and only if there exists a production of the form $U \rightarrow x S V y$, for some U, x, V, and y and there exists a derivation of the form $V \rightarrow Tz$ for some z.
- c) For any ordered pair of symbols (S,T), relation $S \rightarrow T$ holds if and only if (1) there exists a production of the form $U \rightarrow x V T y$, for some U, x, V, y and there exists a derivation of the form $V \rightarrow z S$ for some z; or (2) there exists a production of the form $U \rightarrow x V W y$, for some x, V, W, y and there exists derivations of the form $V \rightarrow u S$ and $W \rightarrow T v$ for some u, v.

In order to simplify the algorithm for constructing the precedence matrix, the definitions of left (or right) part of a non-terminal symbol S are now introduced.

The left (or right) part of a non-terminal symbols S is a set of symbols T_i (either terminal or non-terminal) with the following properties:

- a) They are the leftmost (or rightmost) symbol of the right part of a production relative to S :

$$S \rightarrow T_i x \text{ (or } S \rightarrow x T_i \text{)}$$

- b) They belong to the left (or right) part of a non-terminal S_1 which in turn satisfies condition a:

$$S \rightarrow S_1 x \text{ (or } S \rightarrow x S_1 \text{)} \text{ and } S_1 \rightarrow T_i y \text{ (or } S_1 \rightarrow y T_i \text{)}$$

The algorithm for constructing the precedence matrix consists in a search on the productions of the grammar looking for the left and right parts of non-terminal symbols. The algorithm can be outlined as follows: starting with the first production of the grammar and the first pair of adjacent symbols of the production, and scanning all the adjacent symbols and all productions:

- assign relation $\hat{=}$ to the position in the matrix relative to the symbols in question;
- if the second symbol of the pair is non-terminal, assign relation $\hat{<}$ to the positions in the matrix relative to the line of the first symbol and to the columns of the symbols belonging to the left part of the second symbol of the pair;
- if the first symbol of the pair is non-terminal, assign relation $\hat{>}$ to the positions in the matrix relative to the column of the second symbol and the lines of the symbols belonging to the right of the first symbol of the pair;
- if both symbols of the pair are non-terminal, assign relation $\hat{>}$ to the positions in the matrix relative to the lines corresponding to the right part of the first symbol and the columns corresponding to the left part of the second symbol of the pair.

This part of the algorithm is performed by subroutines PREMAT and PART.

Subroutine PREMAT assigns the adequate relations ~~on~~ ^{to} the positions indicated by subroutine PART. The given grammar, upon which the scan is to be made, must conform to the following specifications:

- a) no equal right parts are allowed in two or more different productions;
- b) the right part of the production relative to the axiom must be delimited by terminal symbols which can not appear in any other production;

On the programs that follow, three other restrictions are made:

- c) the delimiter mentioned in b must be the last symbol of the vocabulary when input is made;
- d) the production relative to the axiom must be of the form $S \rightarrow 'T'$, where S can not appear in a right part of any other production.
- e) All the symbols used are restricted to be one character in length.

Subroutine PART finds the left or right parts of a given non-terminal. The set of symbols found is stored in a vector.

This subroutine uses two stacks, one for the non-terminal symbols found during the search and the other for the number of the production being scanned. Each non-terminal found during the search is stacked and the subroutine tries to find its corresponding left (or right) part. When all the productions relative to the symbol in the top of the stack have been scanned out, the stacks are popped up and the search continues relative to the new top symbol. The search stops when the stack is empty.

Before each assignment is made subroutine PREMAT checks to see if the position in question is already occupied.

3. The Parser

Once the grammar is found to be of the precedence type, strings of symbols can be tested. This is made by subroutine PARSER, which executes the canonical parse. This subroutine scans the string looking for the end of a handle and then scans backwards looking for the beginning of the same handle. The last symbol of the handle is the first symbol found in the forward scan for which the relation with its successor is of the \succ type. The first symbol of the handle is the first symbol found in the backward scan for which the relation with its predecessor is of the \prec type.

The productions are then searched for a right part which matches the handle so delimited. This subroutine works with a stack holding the scanned symbols and a vector where the relations of the type \leftarrow found during the forward scan are kept in. The use of this vector avoids the necessity of the backward scan upon the string. Once a handle is replaced, the scan starts at the position immediately after the rightmost element of the replaced handle.

This subroutine checks for input symbols not belonging to the vocabulary and for incorrect sequences of symbols on the given strings.

4. Results

This section presents a listing of the programs (written in FORTRAN IV) and results obtained in an IBM 7044 computer. The grammars used are described in Ref. 1 and Ref. 2, and, for illustrative purposes, are produced at the output of the program, together with their respective vocabularies.

Because of the limited character set of the 7044 system, relations $\hat{=}$, \leftarrow and \rightarrow are represented by the symbols =, * and +. Positions of the precedence matrix filled with zeros represent impossible relations between the corresponding symbols.

References

1. N.Wirth and H. Weber: Euler, a generalization of ALGOL and its formal definition
Part 1. Communications of the ACM, Jan. 66, pp 13-25.
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Feb. 68, pp 77-113
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Mac Donald, ed. 1969.

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0 $IBFTC SC04
C
C THIS IS A PARSER FOR A PRECEDENCE GRAMMAR . IT USES
C THREE SUBPROGRAMS. THE FIRST CONSTRUCTS THE PRECEDENCE
C MATRIX TO BE USED IN THE PARSING. THE SECOND FINDS THE
C LEFT OR RIGHT PARTS OF A PRODUCTION. THE THIRD PARSES
C THE INPUT SENTENCE CHECKING WHETHER THE SENTENCE
C BELONGS TO THE LANGUAGE OR NOT.
C
1 COMMON DEF(20),PRD(20,50),TERMV(50),PRMAT(50,50)
2 COMMON PPART(50),VOC(100),NUM(20),STRING(30)
3 COMMON NPRCD,NTERM,NSYMB,KS
4 INTEGER DEF,PRCD,TERMV,PRMAT,PPART,VOC,STRING
C
C -----INPUT AND OUTPUT OF SYNTAX AND VOCABULARIES-----
C
5 9 READ 1000,NPRCD
7 1000 FORMAT(I5)
10 DO 100 I=1,NPRCD
11 READ 1001,K,DEF(I),(PRCD(I,J),J=1,K)
17 1001 FORMAT(I5,75A1)
20 100 NUM(I) = K
22 READ 1001,NTERM,(TERMV(I),I=1,NTERM)
30 READ 1001,NSYMB,(VOC(I),I=1,NSYMB)
36 PRINT 1020
37 1020 FORMAT(1H=////////)
40 PRINT 1002
41 1002 FORMAT(/15X,24HTHIS IS THE GIVEN SYNTAX/)
42 DO 110 I=1,NPRCD
43 K = NUM(I)
44 110 PRINT 1003,DEF(I),(PRCD(I,J),J=1,K)
52 1003 FORMAT(/15X,A1,3H = ,74A1)
53 PRINT 1004, (VOC(I),I=1,NSYMB)
60 1004 FORMAT(/15X,22HTHIS IS THE VOCABULARY//15X,20(A1,1H,))
61 PRINT 1005, (TERMV(I),I=1,NTERM)
66 1005 FORMAT(/15X,31HTHIS IS THE TERMINAL VOCABULARY//
115X,20(A1,1H,))
C
C -----CONSTRUCTION OF THE PRECEDENCE MATRIX-----
C -----TEST IF GRAMMAR OX-----
C
67 CALL PREMAT(IND)
70 GO TO (1,2,3), IND
71 1 PRINT 1006
72 1006 FORMAT(/15X,145HTHE GIVEN GRAMMAR IS NOT A PRECEDENCE GRAMMAR)
73 CALL EXIT
74 3 PRINT 1007
75 1007 FORMAT(/15X,140HA SYMBOL WAS NOT FOUND IN THE VOCABULARY)
76 CALL EXIT
77 2 PRINT 1008, (VOC(I),I=1,NSYMB)
104 1008 FORMAT(/15X,29HTHIS IS THE PRECEDENCE MATRIX//
121X,30(A1,2H )//)
105 DO 120 I=1,NSYMB

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```

106 120 PRINT 1009, VOC(I), (PRMAT(I,J),J=1,NSYMB)
114 1009 FORMAT(18X,A1,20(2H ,^1)//)
C
C -----INPUT AND PARSE OF STRING TO BE TESTED-----
C
115 7 READ 1010, LASTS, LASTG, KS, (STRING(I), I=1, KS)
125 1010 FORMAT(2I3, I4, 70A1)
126 PRINT 1011, (STRING(I), I=1, KS)
133 1011 FORMAT(///15X, 29HINPUT STRING TO BE TESTED ---, 70A1)
134 CALL PARSE(KEY)
135 GO TO (4,5), KEY
01234 136 01234 PRINT 1012 01234 01234 01234 01234 01234 01234 01234 01234 01234
137 1012 FORMAT(//30X, 36HGIVEN STRING BELONGS TO THE LANGUAGE)
140 GO TO 6
141 5 PRINT 1013
142 1013 FORMAT(//30X,
144HGIVEN STRING DOES NOT BELONG TO THE LANGUAGE)
143 6 IF(LASTS.EQ.1) GO TO 8
146 GO TO 7
147 8 IF(LASTG.EQ.1) CALL EXIT
152 DO 130 I=1, NSYMB
153 DO 130 J=1, NSYMB
154 130 PRMAT(I,J) = 0
157 GO TO 9
160 END

```

```

081207SRCASERGIO CARVALHO
IBMAP ASSEMBLY SC04

NO MESSAGES FOR ABOVE ASSEMBLY

1 2 3 4 5 6
0123456789 0123456789 0123456789 0123456789 0123456789 0123456789 0123456789 0123456789

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```

0 $IBFTC SC01
1 SUBROUTINE PRMAT(IND)
C
C THIS SUBROUTINE CONSTRUCTS THE PRECEDENCE MATRIX
C RELATIVE TO THE GIVEN GRAMMAR. THE MATRIX(PMAT) WILL
C CONSIST OF THE SYMBOLS =,+,*. EACH TIME A NEW SYMBOL
C IS TO BE PUT INTO THE MATRIX, A TEST IS MADE TO SEE
C IF THE POSITION BEING CONSIDERED IS ALREADY OCCUPIED.
C THIS BEING THE CASE, A MESSAGE IS PRINTED INDICATING
C POSITION AND SYMBOLS IN QUESTION. ALSO, PARAMETER
C IND IS SET TO 1 MEANING THAT THE GIVEN GRAMMAR IS NOT
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 A PRECEDENCE GRAMMAR. THIS SUBROUTINE USES SUBROUTINE
C PART, WHICH DETERMINES THE SYMBOLS BELONGING TO THE
C LEFT OR RIGHT PARTS OF A GIVEN SYMBOL.
C
2 COMMON DEF(20), PROD(20,50), TERMV(50), PMAT(50,50)
3 COMMON PPART(50), VOC(100), NUM(20), STRING(30)
4 COMMON NPROD, NTERM, NSYMB, KS
5 INTEGER DEF, PROD, TERMV, PMAT, PPART, VOC, AUX(50), STRING
6 DATA IEQ, IPREC, ISUC/1H=, 1H*, 1H+/
C
C -----SET INITIAL VALUES-----
C
7 IND = 2
10 KT = 0
11 I = 1
C
C -----TEST IF PRODUCTION HAS MORE THAN ONE SYMBOL-----
C -----IF NOT, GET ANOTHER PRODUCTION-----
C
12 2 IF(NUM(I).GT.1) GO TO 1
15 22 IF(I.EQ.NPROD) RETURN
20 I = I + 1
21 GO TO 2
C
C -----IDENTIFY SYMBOLS TO BE CONSIDERED-----
C
22 1 J = 1
23 23 M = 1
24 DO 110 K1=1,NSYMB
25 IF(PROD(I,J).EQ.VOC(K1)) GO TO 3
30 110 CONTINUE
32 NS = PROD(I,J)
33 GO TO 5
3 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 H
34 DO 120 K2=1,NSYMB
35 IF(PROD(I,J+1).EQ.VOC(K2)) GO TO 4
40 120 CONTINUE
42 NS = PROD(I,J+1)
C
C -----SYMBOL NOT FOUND IN THE VOCABULARY-----
C
43 5 PRINT 50, NS
44 50 FORMAT(//30X,6HSYMBOL,'X',A1,3X,
123HNOT FOUND IN VOCABULARY)
45 IND = 3

```

46	RETURN				
C					
C		-----THIS IS THE APPLICATION OF RULE A (SEE TEXT).-----			
C		-----TEST IF POSITION EMPTY . IF SO , PUT = SIGN-----			
C		-----IF NOT , PRINT MESSAGE AND RETURN IND=1-----			
C					
47	4 IF (PRMAT(K1,K2).EQ.0)GO TO 6				
52	PRINT 51, K1,K2,PRMAT(K1,K2)				
53	51 FORMAT(/30X,9HPOSITION(,I3,1H,,I3,15H)OCCUPIED WITH , 1A1,5H SIGN)				
54	IND = 1				
01234	55 GO TO 7				
56	6 PRMAT(K1,K2) = IEQ				
C					
C		-----THIS IS THE APPLICATION OF RULES B AND C-----			
C		-----THE RULE TO BE APPLIED DEPENDS ON THE VALUE OF M-----			
C					
57	7 IF(M.EQ.1)GO TO 8				
C					
C		-----TEST IF SYMBOL IS TERMINAL . IF NOT , CALL PART--			
C		-----TO FIND THE LEFT OR RIGHT PART OF SYMBOL-----			
C					
62	17 IF(K1.GT.(NSYMB-NTERM)) GO TO 9				
65	ISYM = VOC(K1)				
66	GO TO 11				
67	8 IF(K2.GT.(NSYMB-NTERM)) GO TO 12				
72	ISYM = VOC(K2)				
73	11 CALL PART(M,ISYM,N)				
C					
C		-----IDENTIFY SYMBOLS TO BE CONSIDERED-----			
C					
74	DO 130 K3=1,N				
75	DO 140 K4=1,NSYMB				
76	IF(PPART(K3).EQ.VOC(K4)) GO TO 10				
101	140 CONTINUE				
103	NS = PPART(K3)				
104	GO TO 5				
C					
C		-----FILL IN APPROPRIATE POSITIONS IF NOT OCCUPIED-----			
C					
105	10 IF(M.EQ.1)GO TO 13				
110	IF (PRMAT(K4,K2).NE.0)GO TO 14				
113	PRMAT(K4,K2) = ISUC				
114	GO TO 130				
01234	115 GO TO 13				
120	PRMAT(K1,K4) = IPREC				
121	GO TO 130				
122	14 PRINT 51, K4,K2,PRMAT(K4,K2)				
123	IND = 1				
124	GO TO 130				
125	15 PRINT 51, K1,K4,PRMAT(K1,K4)				
126	IND = 1				
127	130 CONTINUE				
C					
C		-----TEST IF RULE B (M=1) OR RULE C (M=2) APPLIED-----			

131	C	IF(M.EQ.2) GO TO 16			
134		24 M = 2			
135		GO TO 17			
	C	-----THIS IS THE APPLICATION OF RULE D (SEE TEXT)-----			
136	C	16 IF(KT.EQ.0)GO TO 18			
141		KT = 0			
142		GO TO 9			
	C	-----FIND LEFT PART OF APPROPRIATE SYMBOL AND STORE-----			
	C	-----IT IN AUXILIARY VECTOR-----			
143		18 CALL PART (1,VOC(K2),N1)			
144		DO 150 K5=1,N1			
145		DO 160 K6=1,NSYMB			
146		IF(PPART(K5).EQ.VOC(K6)) GO TO 19			
151		160 CONTINUE			
153		NS = PPART(K5)			
154		GO TO 5			
155		19 AUX(K5) = K6			
156		150 CONTINUE			
	C	-----FIND RIGHT PART OF SYMBOL IN QUESTION AND PUT +			
	C	-----SIGN INTO MATRIX, IF POSITION NOT OCCUPIED-----			
	C				
160		CALL PART(2,VOC(K1),N2)			
161		DO 170 K7=1,N2			
162		DO 180 K8=1,NSYMB			
163		IF(PPART(K7).EQ.VOC(K8)) GO TO 20			
166		180 CONTINUE			
170		NS = PPART(K7)			
171		GO TO 5			
172		20 DO 190 K9=1,N1			
173		L = AUX(K9)			
174		IF(PMAT(K8,L).EQ.0)GO TO 21			
177		PRINT 51,K8,L,PMAT(K8,L)			
200		INC = 1			
201		GO TO 190			
202		21 PMAT(K8,L) = ISUC			
203		190 CONTINUE			
205		170 CONTINUE			
	C	-----TEST IF END OF PRODUCTION-----			
207	C	9 IF(J.EQ.(NUM(I)-1)) GO TO 22			
212		J = J + 1			
213		GO TO 23			
214		12 KT = 1			
215		GO TO 24			
216		ENC			

```

0 $IBFTC SC02
1  SUBROUTINE PART(M,ISYM,N)
C
C  THIS SUBROUTINE FINDS THE LEFT (M=1) OR RIGHT (M=2)
C  PARTS OF A NON-TERMINAL SYMBOL. VECTOR PPART HOLDS
C  THE N SYMBGLS FOUND. THIS SUBROUTINE USES TWO STACKS
C  ONE FOR THE SYMBOL BEING CONSIDERED AND OTHER FOR THE
C  INDEX OF THE PRODUCTION IN QUESTION. IF A NON-TERMINAL
C  IS FOUND TO BE IN PPART, IT IS STACKED AND THE PROGRAM
C  TRIES TO FIND ITS LEFT(OR RIGHT) PART. WHEN ALL THE
C  PRODUCTIONS HAVE BEEN SCANNED, A TEST IS MADE TO SEE
0 1 2 3 4 5 6 7 8 0 1 2 3 4 IF THE STACK IS EMPTY, IF NOT, THE SCAN CONTINUES.
C  IF EMPTY, RETURN.
C
2  COMMON DEF(20),PROD(20,50),TERMV(50),PRMAT(50,50)
3  COMMON PPART(50),VOC(100),NUM(20),STRING(30)
4  COMMON NPROD,NTERM,NSYMB,KS
5  INTEGER DEF,PROD,TERMV,PRMAT,PPART,VOC,STS(20),STP(20)
6  INTEGER STRING
C
C  -----SET INITIAL VALUE-----
7  I = 1
10 N = 0
11 STS(I) = ISYM
12 8 STP(I) = 2
13 L = STP(I)
C
C  -----FIND A PRODUCTION RELATIVE TO SYMBOL IN QUESTION-----
14 3 IF(DEF(L).EQ.STS(I)) GO TO 1
C
C  -----TEST IF END OF PRODUCTIONS-----
17 7 IF(L.EQ.NPROD) GO TO 2
22 L = L + 1
23 GO TO 3
C
C  -----FIND APPROPRIATE PART OF PRODUCTION-----
24 1 STP(I) = L
25 IF(M.EQ.1)GO TO 4
30 1L = NUM(L)
31 IT = PROD(L,1L)
0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8
32 8 0 1 2 3 4 GO TO 5
33 4 IT = PROD(L,1)
C
C  -----TEST IF SYMBOL ALREADY IN PPART.-----
34 5 IF(N.EQ.0)GO TO 6
37 DO 120 K2=1,N
40 IF(IT.EQ.PPART(K2)) GO TO 7
43 120 CONTINUE
45 6 N = N + 1
46 PPART(N) = IT

```


0	#IBFTC SC03				
1	SUBROUTINE PARSER(KEY)				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
	C				
2	COMMON DEF(20),PROD(20,50),TERMV(50),PRMAT(50,50)				
3	COMMON PPART(50),VOC(100),NUM(20),STRING(30)				
4	COMMON NPROD,NTERM,NSYMB,KS				
5	INTEGER DEF,PROD,TERMV,PRMAT,PPART,VOC,STRING,				
	ISTACKS(30),STACKP(30),DEL				
6	DATA DEL/'H*/',ISUC,IPRFC,IEQ/'H+',IH*,'H=/'				
	C				
	C				
	C				
	C				
7	IF(STRING(1).EQ.DEL) GO TO 1				
12	3 PRINT 1000				
13	1000 FORMAT(/'30X,				
	14HINPUT STRING CONTAINS UNIDENTIFIED SYMBOL)				
14	6 KEY = 2				
15	RETURN				
	C				
	C				
	C				
	C				
16	1 STACKS(1) = DEL				
17	K1 = NSYMB				
20	K = 2				
21	J = 2				
	C				
	C				
	C				
	C				
22	10 DO 120 K2=1,NSYMB				
23	IF(STRING(K).EQ.VOC(K2)) GO TO 2				
26	120 CONTINUE				
30	GO TO 3				
	C				
	C				
	C				
	C				
	C				
31	2 IF(PRMAT(K1,K2).EQ.ISUC) GO TO 4				
34	IF(PRMAT(K1,K2).EQ.IPRFC) GO TO 7				
37	IF(PRMAT(K1,K2).EQ.IEQ) GO TO 5				
42	PRINT 1001				
43	1001 FORMAT(/'30X,28HINCORRECT SEQUENCE ON STRING)				
44	GO TO 6				

45	7	STACKP(J) = IPREC				
46	5	STACKS(J) = STRING(K)				
	C					
	C	-----TEST IF END OF STRING. IF SQ, TEST CONTENTS OF-----				
	C	-----STACK. IF NOT, PREPARE NEXT SEARCH-----				
	C					
47		IF(K.LT.KS) GO TO 8				
52		IF(STACKS(2).EQ.VOC(1).AND.STACKS(3).EQ.DEL) GO TO 9				
55		PRINT 1002				
56	1002	FORMAT(//30X,20HINCOMPLETE REDUCTION)				
57		GO TO 6				
60	9	KEY = 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0				
61		RETURN				
62	8	J = J + 1				
63		K = K + 1				
64		K1 = K2				
65		GO TO 10				
	C					
	C	-----SEARCH RELATION IPREC IN AUXILIARY VECTOR-----				
	C					
66	4	M = J - 1				
67	12	IF(STACKP(M).EQ.IPREC) GO TO 11				
72		M = M - 1				
73		GO TO 12				
74	11	N = M				
75		L = 2				
76		I = 1				
	C					
	C	-----SEARCH ADEQUATE PRODUCTION-----				
	C					
77	15	IF(PROD(L,I).EQ.STACKS(N)) GO TO 13				
102		IF(L.EQ.NPROD) GO TO 14				
105		L = L + 1				
106		I = 1				
107		N = M				
110		GO TO 15				
111	14	PRINT 1003				
112	1003	FORMAT(//30X,31HNO PRODUCTIONS MATCH THE HANDLE)				
113		GO TO 6				
114	13	IF(N.EQ.(J-1)) GO TO 16				
117		N = N + 1				
120		I = I + 1				
121		GO TO 15				
	C					
	C	2----- REPLACE HANDLE AND PREPARE NEXT SEARCH-----				
	C					
122	16	STACKS(M) = DEF(L)				
123		J = M + 1				
124		DO 130 K3=1,NSYMB				
125		IF(STACKS(M-1).EQ.VOC(K3)) GO TO 17				
130	130	CONTINUE				
132		GO TO 3				
133	17	DO 140 K4=1,NSYMB				
134		IF(STACKS(M).EQ.VOC(K4)) GO TO 18				
137	140	CONTINUE				
141		GO TO 3				

THIS IS THE GIVEN SYNTAX

S = 'T'

T = U)

U = (

U = UI

0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8 0 1 2 3 4 5 6 7 8

U = UT

THIS IS THE VOCABULARY

T, U,), (, I, '.

THIS IS THE TERMINAL VOCABULARY

), (, I, '.

THIS IS THE PRECEDENCE MATRIX

	T	U)	(I	'
T	+	+	+	+	+	=
U	=	*	=	*	=	0
)	+	+	+	+	+	+
(+	+	+	+	+	0
I	+	+	+	+	+	0
'	=	*	0	*	0	0

INPUT STRING TO BE TESTED ----'(T)'

GIVEN STRING BELONGS TO THE LANGUAGE

INPUT STRING TO BE TESTED ----'(U())'

GIVEN STRING BELONGS TO THE LANGUAGE

INPUT STRING TO BE TESTED ----'((I(I)))'

GIVEN STRING BELONGS TO THE LANGUAGE

INPUT STRING TO BE TESTED ----'()'.

THIS IS THE GIVEN SYNTAX

$S = T$

$T = U$

$U = V$

$U = U+V$

$V = W$

$W = X$

$W = W*X$

$X = (T)$

$X = I$

THIS IS THE VOCABULARY

T, U, V, W, X, I, +, *, (,), =

THIS IS THE TERMINAL VOCABULARY

I, +, *, (,), =

THIS IS THE PRECEDENCE MATRIX

	T	U	V	W	X	I	+	*	()	=
T	0	0	0	0	0	0	0	0	0	=	=
U	0	0	0	0	0	0	=	0	0	+	+
V	0	0	0	0	0	0	+	0	0	+	+
W	0	0	0	0	0	0	+	=	0	+	+
X	0	0	0	0	0	0	+	+	0	+	+
I	0	0	0	0	0	0	+	+	0	+	+
+	0	0	=	*	*	*	0	0	*	0	0
*	0	0	0	0	=	*	0	0	*	0	0
(0	0	0	0	0	0	+	+	0	+	+
)	0	0	0	0	0	0	+	+	0	+	+
=	=	*	*	*	*	*	0	0	*	0	0

INPUT STRING TO BE TESTED --- 'I'

GIVEN STRING BELONGS TO THE LANGUAGE

INPUT STRING TO BE TESTED --- 'I+I+I'

GIVEN STRING BELONGS TO THE LANGUAGE

INPUT STRING TO BE TESTED ---'I*I'							
INCORRECT SEQUENCE ON STRING							
GIVEN STRING DOES NOT BELONG TO THE LANGUAGE							
INPUT STRING TO BE TESTED ---'({I*I})+I*I'							
1	2	3	4	5	6	7	8
0	1	2	3	4	5	6	7
GIVEN STRING BELONGS TO THE LANGUAGE							
INPUT STRING TO BE TESTED ---'({I+I})'							
INCORRECT SEQUENCE ON STRING							
GIVEN STRING DOES NOT BELONG TO THE LANGUAGE							
INPUT STRING TO BE TESTED ---'({(I+I)*I})+I'							

GIVEN STRING BELONGS TO THE LANGUAGE

081207SRCASERGIO CARVALHO							
081207SRC TEMP TOTAL 000178 SEG - TEMP EKEG. 00002L SEG - CART LIDOS 00							